

# Formal Verification and Simulation: Co-Verification for Subway Control Systems

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- 1 Introduction
- 2 Methodology
- 3 Requirements of Platform Screen Doors System (PSDS)
- 4 Models
- 5 Formal Verification and Simulation
- 6 Refinement
- 7 Conclusion and Future Work

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- ③ **Matlab Simulink:** Simulink supports linear and non-linear systems, continuous time, sampled time, or a hybrid of the two.
- ④ **Matlab Stateflow:** Stateflow works with Simulink, interactive graphical design, event-driven systems, transitions in response to events and conditions. ( fan, motor, or pump, etc.).

# Hybrid Automata

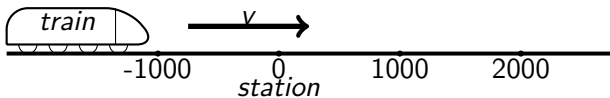


Figure: A train on a line.



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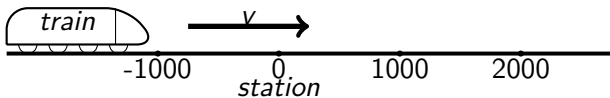


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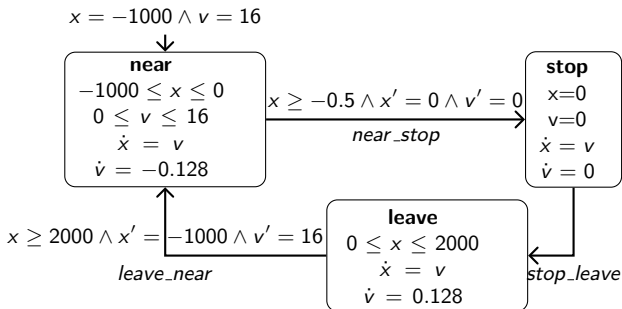


Figure: Train automaton.

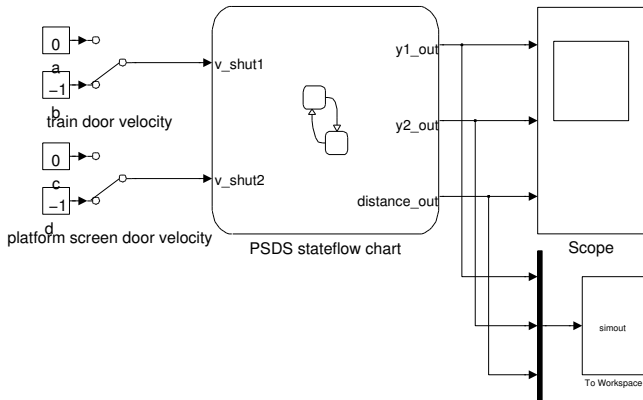


Figure: Simulink model of PSDS.

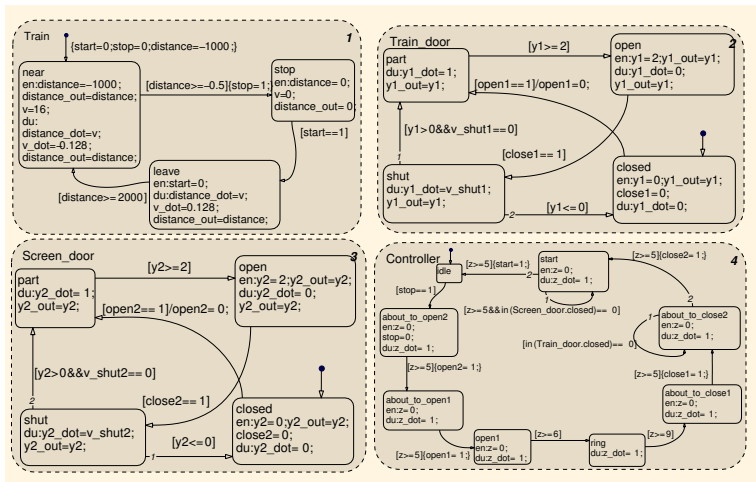


Figure: Stateflow chart of PSDS.

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## Base Phase:

Construct models by formal method and simulation technology, respectively. Liveness properties, coarse-grained.

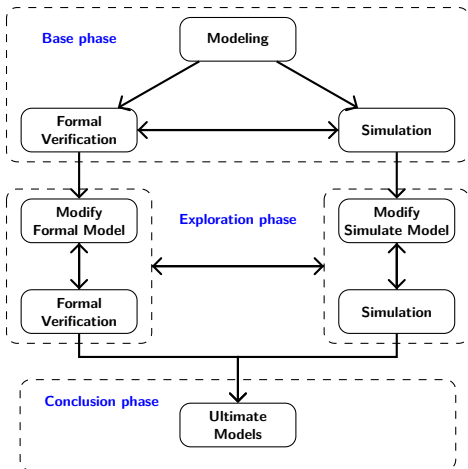


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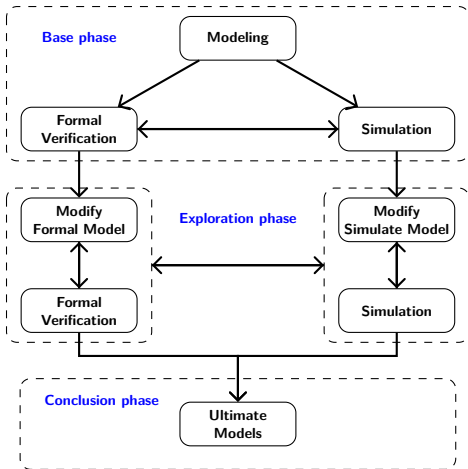


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## Conclusion Phase:

Final models selection.

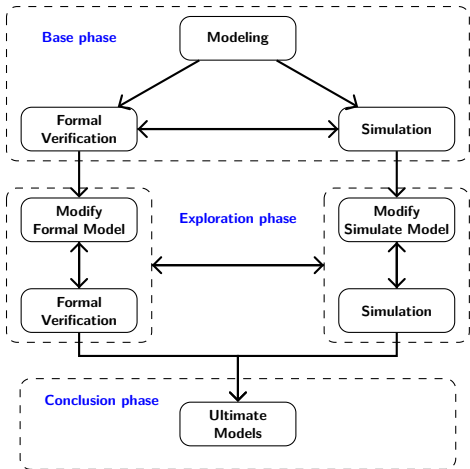


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- ③ **Train Doors First (TDF):** First, close the train doors. And then close the platform screen doors.

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# Train Doors Automaton

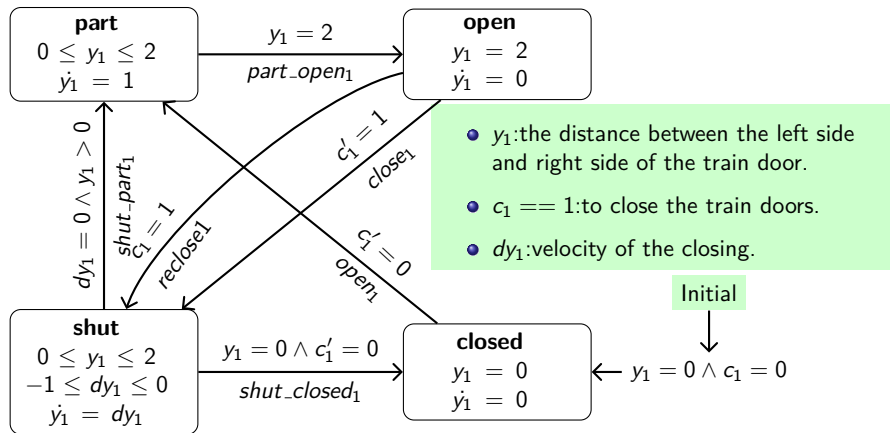


Figure: Train doors automaton.

# Train Doors Chart

- open1: local variable, as a shared variable between train doors and controller.
- v\_shut1: the velocity of closing.
- y1\_out: output variable for plotting in the Scope.
- transition: event[condition]condition\_action/transition\_action.

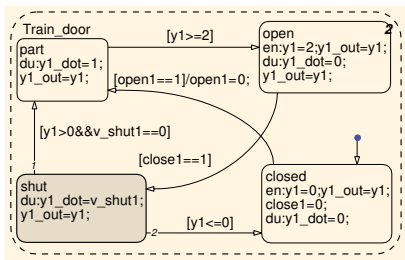


Figure: Train doors chart

# Controller Automaton

- $z$ : stop watch.
- Synchronization labels:
  - open2: open the platform screen doors.
  - open1: open the train doors.
  - close1: close the train doors.
  - close2: close the platform screen doors.

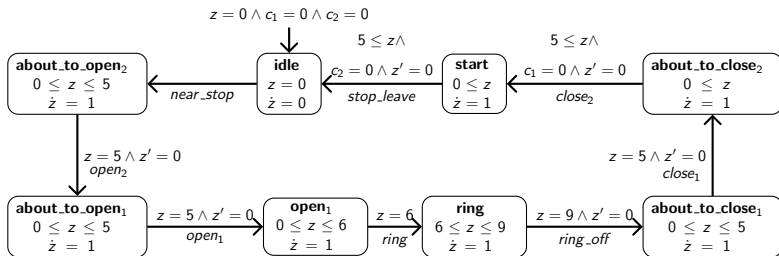


Figure: Controller automaton.

# Controller Chart

- $\text{in}(\text{Train\_door.closed})$ : denotes whether train doors are closed.

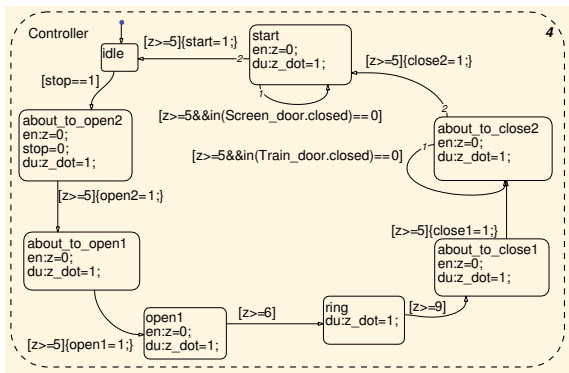


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The train doors need to be closed at first, and then the platform screen doors.

## Property 4: Operation of Doors

There are no operations of doors when the train is running.

## One Normal Running:

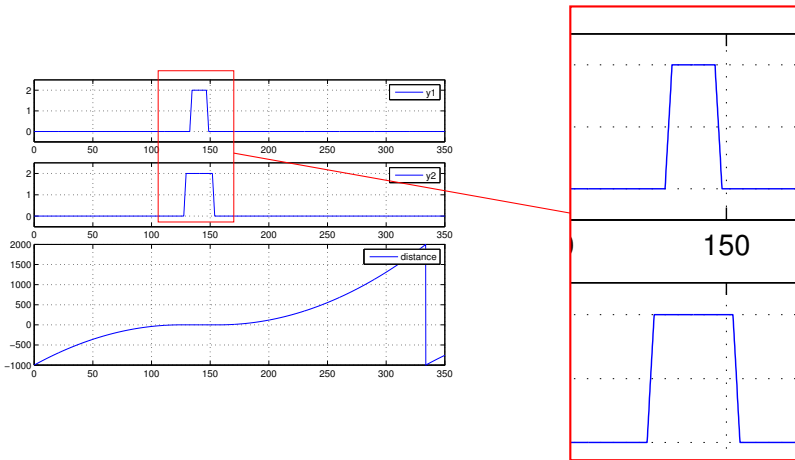


Figure: One normal running.

# Sandwich Simulation

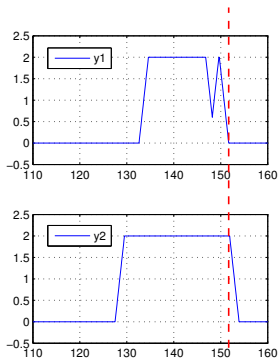


Figure: Sandwich simulation.

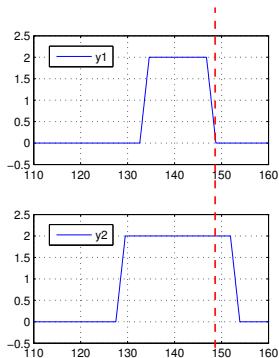


Figure: Normal simulation.

The platform screen doors begin to close almost at the moment the train doors closed.



# Analyze the Sandwich Situation

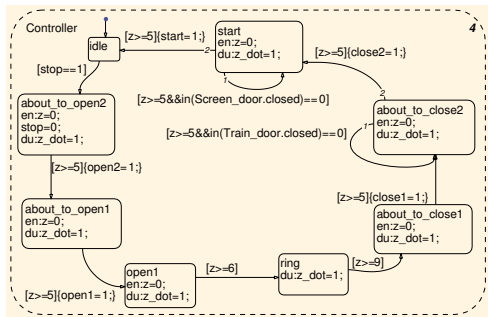


Figure: Controller chart

If the train doors are closed when  $z == 4.9$ , then the predicate  $\text{in}(\text{Train\_door.closed}) == 0$  is false. Thus, the transition from **about\_to\_close2** to **start** will occur when  $z$  is 5, the time interval is 0.1s.

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# Simulation Refinement

Remove  $z \geq 5$  in the predicate  $z \geq 5 \ \&\& \ in(Train\_door.closed) == 0$ :

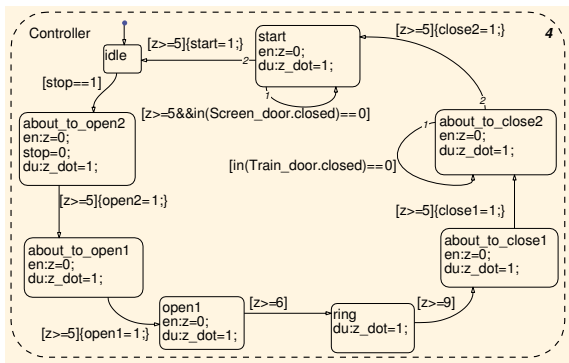


Figure: Refined Controller chart.

# Simulation after Refinement

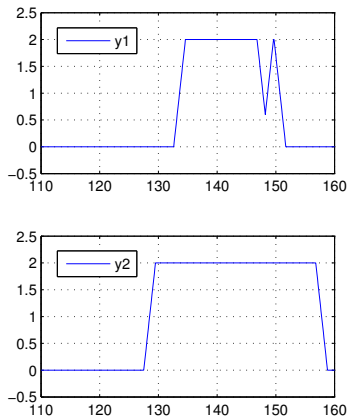


Figure: Simulation after the refinement.

# Formal Verification Refinement

Add a self-loop control switch of mode *about\_to\_close<sub>2</sub>* in the controller automaton. *shut\_closed<sub>1</sub>* is the synchronization label between train doors automaton and controller automaton.

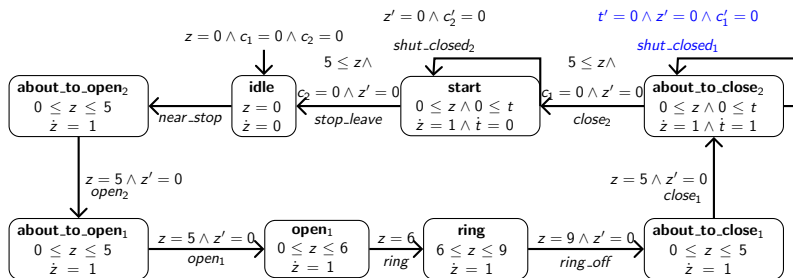


Figure: Refined Controller automaton.

# Verification after Refinement

The system is represented by:

$sys = controller \& traindoor \& screendoor \& train.$

The following states are not reachable in the system:

$sys.\{start \sim \$ \sim \$ \sim \$ \& t < 5\}.$

All states when the controller is in mode *start*:

```
controller ~ traindoor ~ screendoor ~ train. {
  start ~ closed ~ shut ~ stop &
  -1 <= dy2 <= 0 & 0 <= y2 <= 2 & x == 0 & y1 == 0 &
  close2.flag == 1 & close1.flag == 0 &
  t >= 5 & z + y2 >= 2,
  start ~ closed ~ open ~ stop &
  x == 0 & y2 == 2 & y1 == 0 & close2.flag == 1 &
  close1.flag == 0 & t >= 5 & z >= 0,
  start ~ closed ~ closed ~ stop &
  x == 0 & y2 == 0 & y1 == 0 & close2.flag == 0 &
  close1.flag == 0 & t >= 5 & z >= 0,
  start ~ closed ~ part ~ stop &
  0 < y2 <= 2 & x == 0 & y1 == 0 & close2.flag == 1 &
  close1.flag == 0 & t >= 5 & z + y2 >= 2 }.
```

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## Conclusion

- Feedback-Advancement Verification: Combine formal verification with simulation.
- Application: Platform Screen Doors System

## Future work, Models Translation

- Co-Verification on subway control systems.
- The Compositional Interchange Format for Hybrid Systems(CIF).  
<http://se.wtb.tue.nl/sewiki/cif/Start>.
- HyLink, translate a subset of Simulink/Stateflow to HyXML format, tools, such as HyTech, UPPAAL, etc.  
<http://hsver.crhc.illinois.edu/index.php/HyLink>.
- Translate to Hybrid Systems Interchange Format(HSIF, XML format),  
<http://wiki.grasp.upenn.edu/hst/index.php?n=Main.HSIF>.



# Thanks

Thank you very much!